

Class: SE (Mech/Auto)

Exam: SE (Mech/Auto) Sem-III (Rev)Sum2010

Code : AN-2432

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Q1.a)

Intensive property: The properties which are independent of mass of system is called as intensive properties. Ex. Temperature, Pressure

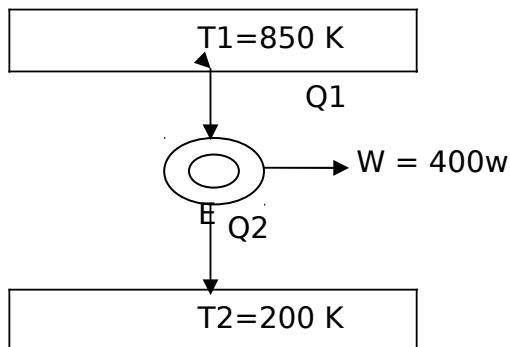
Extensive properties: The properties which are dependent of mass of system is called as extensive properties. Ex. Density, Specific extensive property

b)

1. Practically it is not possible to bring in contact and remove alternately heat reservoir and adiabatic cover.

2. Large variation in speed cannot be obtained in practice.

c)



Rate of heat supplied ,

$$Q_s = 35.5 \text{ kJ/min} = 591 \text{ w}$$

Actual eff. Of engine

$$\begin{aligned} &= \text{Power output / heat supplied} \\ &= 400/591 \\ &= 67.68 \% \end{aligned}$$

Carnot eff.

$$\begin{aligned} &= 1 - (T_2/T_1) \\ &= 1 - (200/850) \end{aligned}$$

$$= 76.47 \%$$

Since eff of engine is less than carnot eff, hence his claim is possible.

d)

$$m = 2 \text{ kg}$$

$$P_0 = 8 \text{ bar}$$

$$X = 0.8$$

from Molier chart

$$h = 2360 \text{ kJ/kg}$$

$$v = 0.2 \text{ m}^3/\text{kg}$$

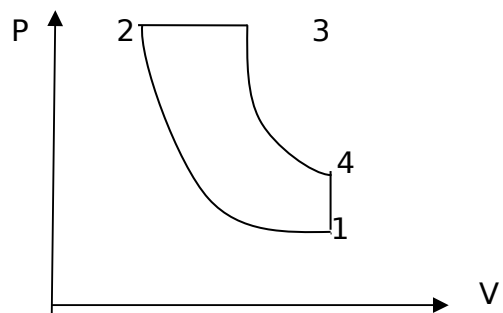
Hence for 2 kg

$$H = 4720 \text{ kJ}$$

$$V = 0.4 \text{ m}^3$$

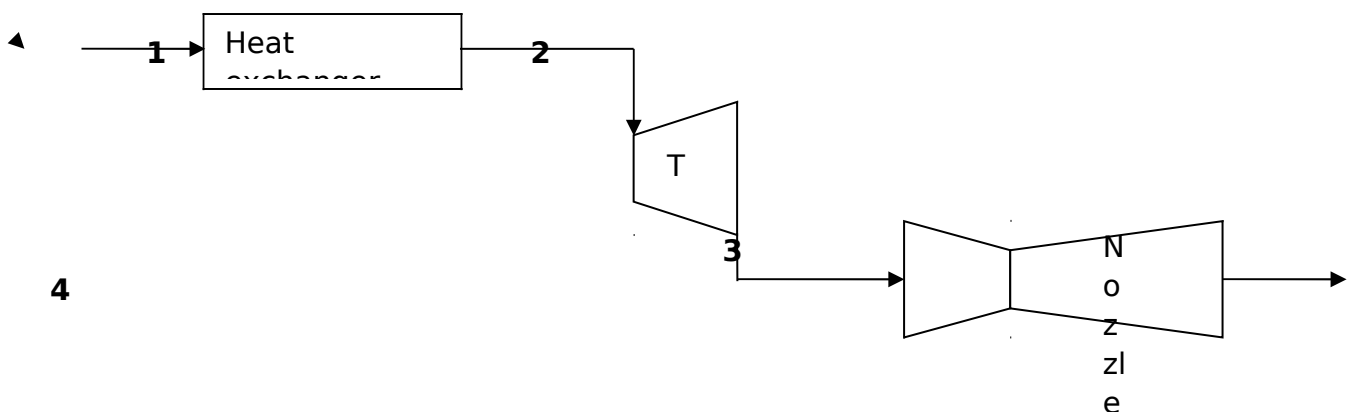
e)

Cut off ratio : It is ratio of volume of gas after heat addition to the volume before heat addition in diesel cycle.



Eff of diesel \propto (1 / cutoff ratio)

Q2.a)



$$T1 = 20^\circ \text{C}$$

$$V1 = 40 \text{ m/s}$$

$$T2 = 820^\circ \text{C}$$

$$V2 = 40 \text{ m/s}$$

$$T3 = 620^\circ \text{C}$$

$$V3 = 55 \text{ m/s}$$

$$T4 = 510^\circ \text{C}$$

$$m = 2.5 \text{ kg/s}$$

SFEE for heat exchanger

$$\begin{aligned} Q_{12} &= m(h_2 - h_1) \\ &= m(T_2 - T_1) \\ &= 2 * 1.005 (820 - 20) \\ &= 1608 \text{ kJ/sec} \end{aligned}$$

SFEE for Turbine,

$$m \left(\frac{V_2^2}{2} + h_2 \right) = m \left(\frac{V_3^2}{2} + h_3 \right) + W_T$$

$$\begin{aligned} W_T &= 2 \left(\frac{40^2 - 55^2}{2} \right) + 2 (1.005(800 - 620)) \\ &= -1.425 + 361.8 \\ &= 360.37 \text{ kJ/sec} \end{aligned}$$

SFEE for nozzle,

$$\left(\frac{V_3^2}{2} + h_3 \right) = \left(\frac{V_4^2}{2} + h_4 \right)$$

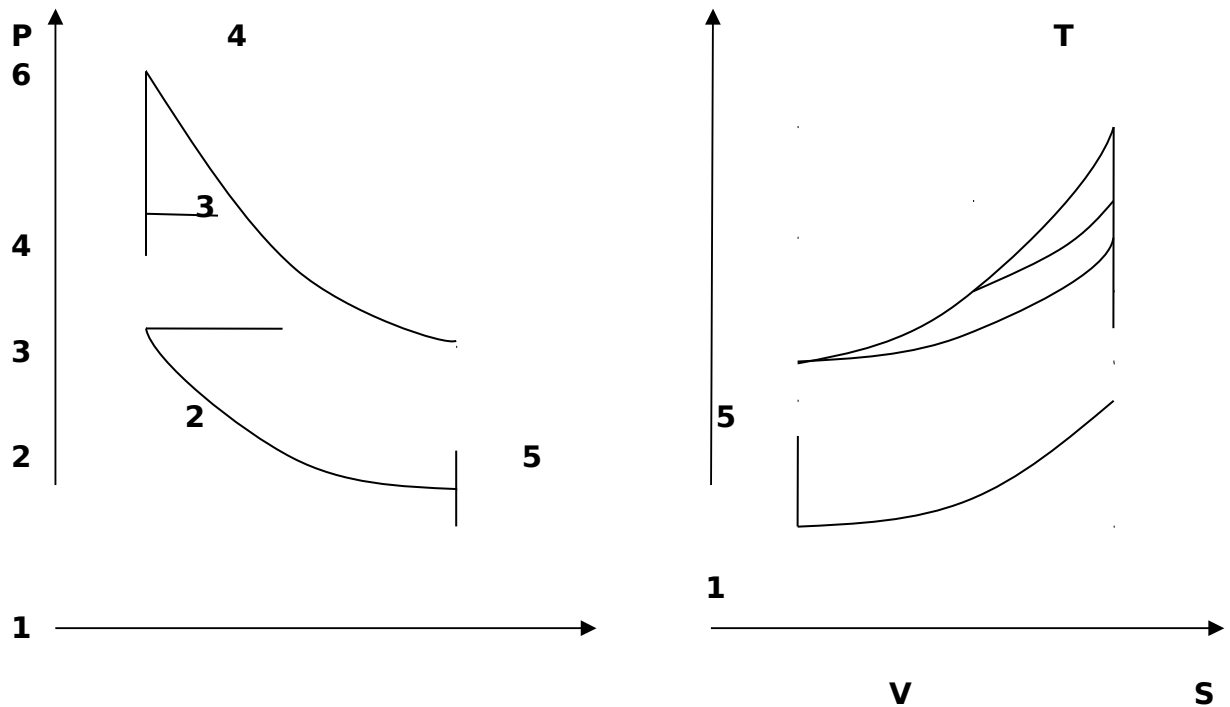
$$V_4 = 471.41 \text{ m/s}$$

Q2.b)

1. Availability: When system is subjected to state change maximum amount of work can be obtained rather than diesel
2. Dead State: When the system is in pressure and temperature equilibrium with surrounding and chemical equilibrium the state of system is known as dead state.
3. Irreversibility: The difference between reversible work and actual work called as irreversibility.

4. Effectiveness: Ratio of actual work to the reversible work called as effectiveness.

Q2.C)



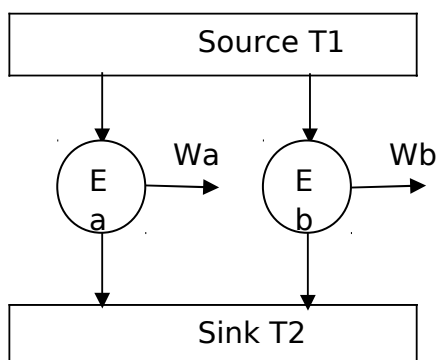
Efficiency of Otto cycle is greater than Efficiency of dual cycle greater than diesel.

Q3.a)

Carnot theorem: It states that no engine has higher efficiency than a reversible engine working between the same constant temperature source and sink.

$$\mu_{\text{carnot}} > \mu_{\text{any engine}}$$

Proof: Let two engines E_a and E_b operating between t_1 and t_2



Let E_a may be any engine, E_b may be reversible engine, let assume, $\mu_a > \mu_b$

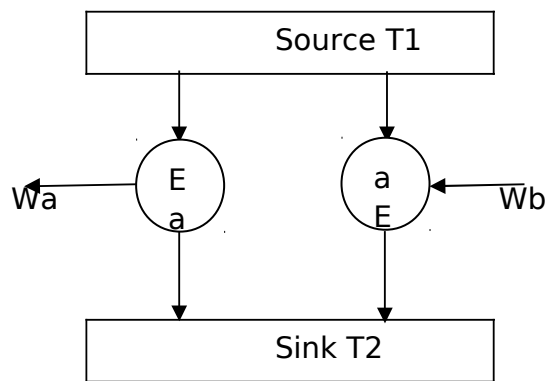
$$Q_{1a} = Q_{1b} = Q_1$$

Since, $\mu_a > \mu_b$

$$W_a / Q_{1a} = W_b / Q_{1b}$$

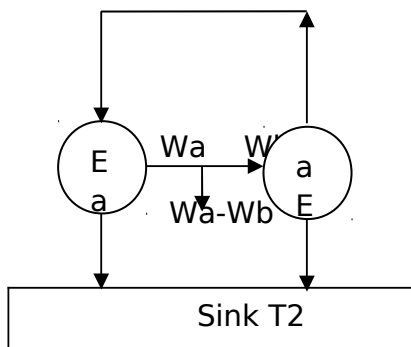
$$W_a = W_b$$

Now let E_b reversed. The magnitude of heat and work remain same but directions are changed.



Since, $W_a > W_b$

Some part of W_a (equal to W_b) may be fed to run engine.



This is not possible.

Hence, $\mu_b > \mu_a$.

Q3. b) Given

$P_1 = 15\text{bar}$

$P_2 = 0.01\text{bar}$

From steam table at 15 bar pressure

$$T_{\text{sat}} = 198.3^{\circ}\text{C}$$

Initial temperature of steam

$$T_1 = 298.3^{\circ}\text{C}$$

Also at 15bar and 298.3°C

$$h_1 = 3034.97\text{kJ/kg.}$$

And $S_1 = 6.913 \text{ kJ/kgK}$

At 0.01bar

$$h_{f2} = h_{f3} = h_3 = 29.3 \text{ kJ/kg}$$

$$h_{fg2} = 2514.4 \text{ kJ/kg}$$

but isentropic efficiency of expansion is 85%

hence, $S_2 = 0.85 S_1$

$$= 5.876 \text{ kJ/kgK}$$

But

$$S_2 = S_{f2} + X_2 * S_{fg2}$$

$$5.876 = 0.106 + X_2 * 8.977$$

$$X_2 = 0.642$$

$$h_2 = h_{f2} + X_2 * h_{fg2}$$

$$= 29.3 + 0.642 * 2514.4$$

$$= 1645.43 \text{ kJ/kg}$$

Pump work

$$W_p = V_{f2} * (P_1 - P_2)$$

$$= 0.001 * (15 - 0.01) * 100000$$

$$= 1.499 \text{ kJ/kg}$$

Turbine work

$$W_t = h_1 - h_2$$

$$= 3034.97 - 1645.54$$

$$= 1389.54 \text{ kJ/kg}$$

Thermal Eff.

$$\begin{aligned} \mu &= (W / Q_s) \\ &= (W_t - W_p) / (h_1 - h_4) \\ &= (1389.54 - 1.499) / (3034.97 - h_4) \end{aligned}$$

Pump work

$$W_p = h_4 - h_3$$

$$h_4 = 30.79$$

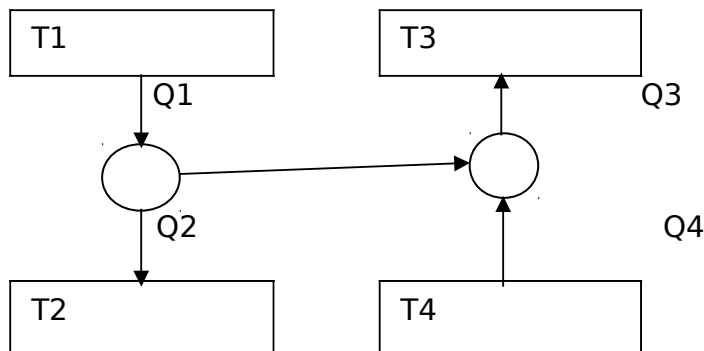
$$\mu_{th} = 46.20 \%$$

Q3.C)

Joule Thomson Coefficient : Throttling process is frequently encountered. In such case enthalpy remain constant. We could find $(\delta t / \delta p)_h$ is a constant. This constant is called as Joule Thomson coefficient.

Region where it is positive is called as cooling region and region where it is negative called as heating region.

Q4.a)



Let output of engine will be W_1 ,

$$W_1 = Q_1 - Q_2 \quad \text{-----I}$$

But, $(Q_1 / T_1) = (Q_2 / T_2)$

$$Q_2 = (T_2 / T_1) * Q_1$$

$$W_1 = Q_1 - (T_2 / T_1) * Q_1 \quad \text{-----II}$$

This work is supplied to heat pump

$$Q_3 = Q_4 + W_1$$

$$= Q_4 + Q_1 * (T_2 / T_1) \text{ -----III}$$

But $(Q_3 / T_3) = (Q_4 / T_4)$

$$Q_3 = (T_3 / T_4) * Q_4$$

Substituting in equation III

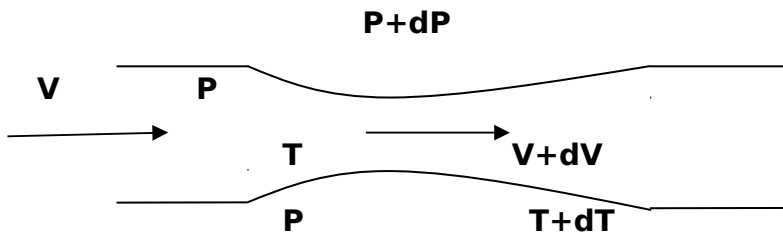
$$(T_3 / T_4) * Q_4 = Q_4 + Q_1 (1 - (T_2 / T_1))$$

$$((T_3 / T_4) - 1) * Q_4 = (1 - (T_2 / T_1)) * Q_1$$

$$Q_4 / Q_3 = (1 - (T_2 / T_1)) / ((T_3 / T_4) - 1)$$

$$Q_4 / Q_3 = T_4 (T_1 - T_2) / T_1 (T_3 - T_4)$$

Q4. b)



$$H_o = h + (V^2 / 2)$$

$$dh = -VdV$$

From property relation

$$Tds = dh - V dp$$

From isentropic flow

$$dh = dp / \rho$$

from above equation,

$$dp = -\rho v Dv$$

$$dp / dV < 0$$

continuity equation gives,

$$W = \rho * A * V$$

By logarithmic differentiation

$$(d \rho / \rho) + (dA / A) + (dV / V) = 0$$

$$(dA / A) = (dV / V) - (d \rho / \rho)$$

$$(dA / A) = (dp / \rho * V^2) (1 - V^2(d\rho / dp))$$

$$(dA / A) = (dp / dV^2) (1 - M^2)$$

$$(dA / A) = (dV / V) (1 - M^2)$$

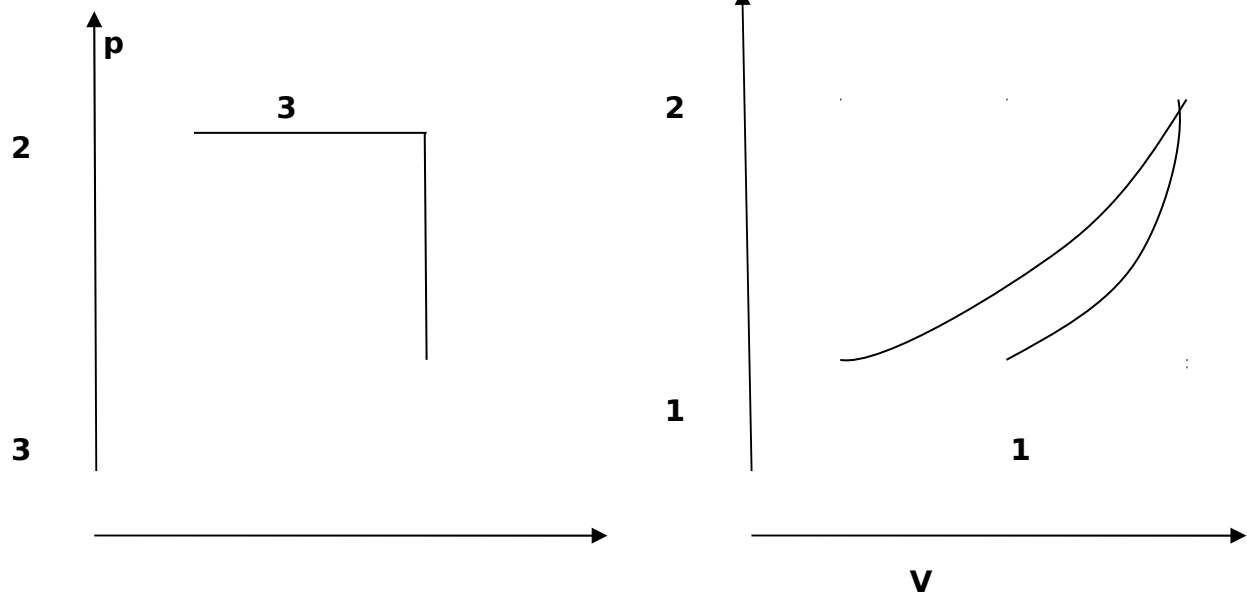
Q4.C)

1) Wet steam : Steam containing mixture of dry steam and water moisture.

2) Quality of steam : It is percentage of dryness of steam.

3) Subcooled liquid: When liquid is cooled under its saturation temperature at certain pressure it is called as subcooled liquid.

Q5.a)



S

$$V_1 = V_2 = 0.05 \text{ m}^3$$

$$P_1 = 1.05 \text{ bar}$$

$$T_1 = T_3 = 293 \text{ K}$$

$$P_2 = 4.5 \text{ bar}$$

$$m = P_1 * V_1 / R * T_1 = 0.0312 \text{ kg}$$

for the process 1-2

$$P_1/T_1 = P_2/T_2$$

$$T_2 = 1255.7 \text{ K}$$

Heat flow

$$Q = Q_{1-2} + Q_{2-3}$$

$$= m C_v (T_2 - T_1) + m C_p (T_3 - T_2)$$

$$= 21.56 - 30.18$$

$$Q = -8.62 \text{ kJ}$$

Net entropy

$$dS = m (C_v \ln(T_2/T_1) + C_p \ln(T_3/T_2))$$

$$= 0.312 (1.044 - 1.462)$$

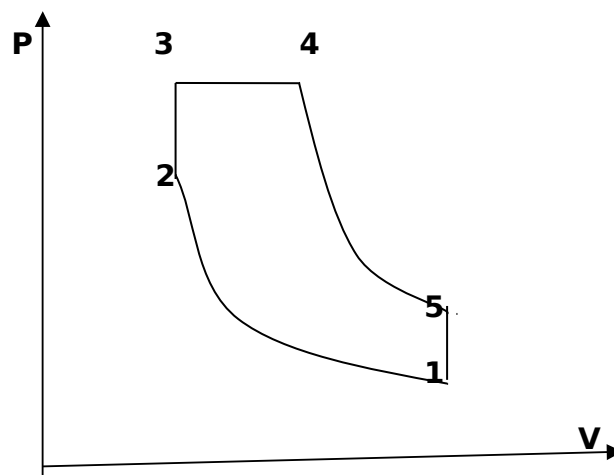
$$dS = - 0.013 \text{ kJ/K}$$

Q5.c)

Variation of back pressure in C-D nozzle

1. If $P=0$, no mass flow of gas
2. If back pressure is reduced as $P_2 > P^*$, the mass flow rate increases.
3. If back pressure is further reduced $P=P^*$, the mass flow rate is maximum and velocity at exit become sonic.
4. If back pressure is further lowered $P < P^*$, mass flow rate remain maximum.

Q6.a)



$$P_1 = 1 \text{ bar}$$

$$T_1 = 363 \text{ K}$$

$$r = 9$$

$$P_4 = 68 \text{ bar}$$

$$Q = 1750 \text{ kJ}$$

Process 1-2,

$$T2/T1 = (V1/V2)^{\gamma-1} = 9^{0.4}$$

$$T2 = 874.18 \text{ K}$$

$$P2 = P1 * (V1/V2)^{\gamma}$$

$$P2 = 21.67 \text{ bar}$$

Process 2-3,

$$T3/T2 = P3/P2$$

$$T3 = 874.18 * (68/21.67)$$

$$T3 = 2743.15 \text{ K}$$

$$Q2-3 = C_v (T3-T2) = 0.718 (2743.15-874.18)$$

$$= 1342.92 \text{ kJ/kg}$$

But,

$$Q3-4 = 1750 - Q2-3$$

$$= 408.07 \text{ kJ/kg} = C_p (T4-T3)$$

$$= 1.005 (T4 - 2743.15)$$

$$T4 = 3149.18 \text{ K}$$

Process 3-4,

$$V4/V3 = T4/T3 = 1.15$$

$$V5/V4 = V1/V2 * V3/V4 = 9 / 1.15$$

$$V5/V4 = 7.83$$

Process 4-5,

$$T5 = T4 * (V4/V5)^{\gamma-1}$$

$$= 1382.58 \text{ K}$$

$$P5 = P1 * (T5/T1)$$

$$= 1 * (1382/363)$$

$$= 3.81 \text{ bar}$$

Efficiency,

$$\mu = 1 - (Q2 / Q1)$$

$$= 1 - (C_v (T5-T1) / ((C_v (T3-T2)) + (C_p(T4-T3))))$$

$$= 58.16 \%$$

Work done,

$$W = Q1 * \mu$$
$$= 1017.18 \text{ kJ/kg.}$$

Q6.b)

let denote x for the properties before shock and y for after shock.

$$m_x = 2$$

$$P_x = 26.5 \text{ kN/m}^2$$

$$\rho_x = 0.413 \text{ kg/m}^2$$

i) P_y , T_y and ρ_y

From gas equation

$$P_x = \rho_x * R * T_x$$

$$T_x = P_x / (R * \rho_x)$$

$$T_x = 223.6 \text{ K}$$

From table at $m = 2$

$$m_y = 0.5774, (P_y/P_x) = 4.5, (\rho_y/\rho_x) = 2.6667, (T_y/T_x) = 1.6875$$

$$(P_{0y}/P_{0x}) = 0.7209 \text{ and } (a_y/a_x) = 1.299$$

Pressure after shock,

$$P_y = 4.5 P_x$$

$$P_y = 119.25 \text{ kPa}$$

Density after shock,

$$\rho_y = 2.667 * \rho_x$$

$$\rho_y = 1.1014 \text{ kg/m}^3$$

temperature after shock,

$$T_y = 1.6875 * T_x$$

$$= 377.3 \text{ K}$$

ii) C_x and C_y (Velocities)

Sonic velocity before shock

$$a_x = \text{SQRT}(r \cdot R \cdot T_x) = \text{SQRT}(1.4 \cdot 287 \cdot 223.6)$$

$$= 299.7 \text{ m/s}$$

$$C_x = m_x \cdot a_x = 599.4 \text{ m/s}$$

$$C_y = m_y \cdot a_y = 224.8 \text{ m/s}$$

iii) Stagnation pressure

$$(P_{ox}/P_x) = (1 + ((r-1)/2)m_x^2)$$

$$P_{ox} = 207.35 \text{ kN/m}^2$$

$$(P_{oy}/P_{ox}) = 72.09$$

$$P_{oy} = 149.48 \text{ kN/m}^2.$$

Q7.a)

Absolute thermodynamic temperature scale:

Eff of Carnot engine is function of temperature alone.

Let consider heat engine working in three pairs of temperature (t_2, t_2) , (t_2, t_3) and (t_1, t_3) when $t_1 > t_2 > t_3$

μ of engine I

$$\mu = 1 - (Q_2/Q_1) = f(t_1, t_2)$$

i.e.

$$(Q_1/Q_2) = f(t_1, t_2)$$

Similarly,

$$(Q_2/Q_3) = f(t_2, t_3)$$

And

$$(Q_1/Q_3) = f(t_1, t_3)$$

From above

$$Q_1/Q_3 = Q_1/Q_2 \cdot Q_2/Q_3$$

$$f(t_1, t_3) = f(t_1, t_2) \cdot f(t_2, t_3)$$

this equation will satisfied if,

$$Q_1/Q_2 = f(t_1, t_2) = \phi(t_1) / \phi(t_2)$$

It follows that if $Q_1 > Q_2$, then $\phi(t_1) > \phi(t_2)$

Hence,

$$t_1 > t_2 .$$

This function is depend on temperature scale.

Therefore we can define $\phi(t)$ itself as temperature on absolute temperature scale.

$$T = \phi(t).$$

Q7.b)

Principle of increase of entropy:

for a process undergone by a system,

$$dS \geq dQ/T$$

for isolated system,

$$(dS)_{iso} \geq 0$$

For reversible process,

$$(dS)_r = 0$$

For irreversible process,

$$(dS) > 0$$

Thus entropy of isolated system like universe never decreases but always increases. This is called as principle of increase of Entropy.

Q7.c)

Rayleigh and Fanno flow:

The flow of compressible gas in a constant area duct with friction and without heat and work transfer is called as Fanno flow.

Q7.d)

Clausius inequality:

Eff of any cycle is equal or less than reversible cycle.

$$1 - (dQ_2/dQ) \leq [1 - (dQ_2/dQ)]_{rev}$$

$$(dQ_2/dQ) \geq (dQ_2/dQ)_{rev}$$

$$(dQ/dQ_2) \leq (dQ/dQ_2)_{rev}$$

But

$$(dQ/dQ_2)_{\text{rev}} = T/T_2$$

$$(dQ_2/dQ) \geq T/T_2$$

Or $dQ/T \leq dQ_2/T_2$

For reversible process

$$dS = dQ_2/T_2$$

for any process

$$dS \geq dQ/T$$

Hence,

$$\oint (dQ/T) \leq \oint dS$$

Since entropy is a property,

$$\oint (dQ/T) \leq 0.$$

It is called as Clausius inequality.